Chapter 3

Multiply by 2-Digit Numbers



Show What You Know

► Practice Multiplication Facts Find the product.

1.
$$8 \times 7 =$$

$$7 \times 8 =$$

2.
$$3 \times (2 \times 4) =$$

$$(3 \times 2) \times 4 =$$

▶ 2-Digit by 1-Digit Multiplication Find the product.

▶ 3- Digit by 1-Digit Multiplication Find the product.

8.
$$672 \times 4$$

10.
$$\times 804 \times 7$$

MATH in the



Yellowstone National Park, which is located in Wyoming, Montana, and Idaho, was America's first National Park. The park has over 500 geysers. Grand Geyser erupts about every 8 hours.

Based on this estimate, how many times would you see this geyser erupt if you could watch it for 1 year? There are 24 hours in a day and 365 days in a year.



Visualize It

Complete the H-diagram using the words with a ✓.

Multiplication Words

Estimation Words

Connect to Vocabulary

Review Words

Associative Property of Multiplication Commutative Property of Multiplication

- ✓ estimate
- ✓ factor
- ✓ partial product
- ✓ place value
- ✓ product regroup
- ✓ round

Preview Words

✓ compatible numbers

Understand Vocabulary

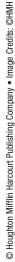
Draw a line to match each word or phrase with its definition.

Word

- **1.** Commutative Property of Multiplication
- 2. estimate
- **3.** compatible numbers
- 4. factor
- **5.** regroup

Definition

- a number that is multiplied by another number to find a product
- to exchange amounts of equal value to rename a number
- to find an answer that is close to the exact amount
- numbers that are easy to compute mentally
- the property that states when the order of two factors is changed, the product is the same.





Multiply by Tens

- Number Sense & Operations 4.NSO.2.2,
- Mathematical Thinking & Reasoning MTR.2.1, MTR.3.1, MTR.4.1, MTR.6.1



UNLOCK the Problem



Animation for a computer-drawn cartoon requires about 20 frames per second. How many frames would need to be drawn for a 30-second cartoon?







The phrase "20 frames per second" means 20 frames are needed for each second of animation. How does this help you know what operation to use?

One Way Use place value.

Multiply. 30×20

You can think of 20 as 2 tens.

$$30 \times 20 = 30 \times$$
_____ tens = ____ tens = 600

Remember

The Associative Property of Multiplication states that you can group factors in different ways and get the same product. Use parentheses to group the factors you multiply first.

Another Way Use the Associative Property.

You can think of 20 as 2×10 .

$$30 \times 20 = 30 \times (2 \times 10)$$

= $(30 \times 2) \times 10$

So, _____ frames would need to be drawn.



MTR Engage in discussions on 4.1 mathematical thinking.

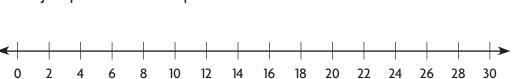
How can you use place value to tell why $60 \times 10 = 600$?

Compare the number of zeros in each factor to the number of zeros in the product. What do you notice?

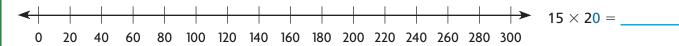
Other Ways

 $oldsymbol{A}$ Use a number line and a pattern to multiply 15 imes 20.

Draw jumps to show the product.







f B Use mental math to find 14 imes 30.

Use the halving-and-doubling strategy.

STEP 1 Find half of 14 to make the problem simpler.

Think: To find half of a number, divide by 2.

STEP 2 Multiply.

nu

STEP 3 Double 210.

Think: To double a number, multiply by 2.

Try This! Multiply.

So, $14 \times 30 = 420$.

Use mental math to find 12 imes 40.

Use place value to find 12×40 .

Share and Show

Math Board

1. Find 20 \times 27. Tell which method you chose. Explain what happens in each step.

2.
$$10 \times 12$$

3.
$$20 \times 20$$

$$\checkmark$$
4. 40 × 24

⊙5.
$$11 \times 60$$



MTR Complete tasks with 3.1 mathematical fluency.

How can you use $30 \times 10 = 300 \text{ to}$ find 30 × 12?

On Your Own

Choose a method. Then find the product.

6.
$$70 \times 55$$

7.
$$17 \times 30$$

8.
$$30 \times 60$$

9.
$$12 \times 90$$

MTR Find the unknown digit in the number.

10.
$$64 \times 40 = 2,56$$

11.
$$29 \times 50 = 1, 150$$

12.
$$3 \times 47 = 1,410$$



- 13. Carmen packs 12 jars of jam in a box. She has 40 boxes. She has 542 jars of jam. How many jars of jam will she have left when all the boxes are full?
- 14. Adelita is preparing for a math contest. Each day, she works on multiplication problems for 20 minutes and division problems for 10 minutes. How many minutes does Adelita practice multiplication and division problems in 15 days?

Problem Solving · Applications Real World

Use the table for 15-16.

- **15. MTR** How many frames did it take to produce 50 seconds of Pinocchio?
- **16.** Are there fewer frames in 10 seconds of *The* Flintstones or in 14 seconds of The Enchanted *Drawing?* What is the difference in the number of frames?
- **17.** The product of my number and twice my number is 128. What is half my number? Explain how you solved the problem.



Title	Date Released	Frames per Second
The Enchanted Drawing [©]	1900	20
Little Nemo [©]	1911	16
Snow White and the Seven Dwarfs [©]	1937	24
Pinocchio [©]	1940	19
The Flintstones [™]	1960–1966	24





18. Tanya says that the product of a multiple of ten and a multiple of ten will always have only one zero. Is she correct? Explain.

19. For numbers 19a-19e, select Yes or No to tell whether the answer is correct.

19a.
$$28 \times 10 = 280$$

19b.
$$15 \times 20 = 300$$

19c.
$$17 \times 10 = 1$$

19c.
$$17 \times 10 = 17$$

19d.
$$80 \times 10 = 800$$

19e.
$$16 \times 30 = 1,800$$

Show the Math

Demonstrate Your Thinking

Multiply by Tens

Go Online Interactive Examples

Choose a method. Then find the product.

1.
$$16 \times 60$$

Use the halving-and-doubling strategy.

Find half of 16:
$$16 \div 2 = 8$$
.

Multiply 60 by this number:
$$8 \times 60 = 480$$
.

Double this result:
$$2 \times 480 = 960$$
.

2.
$$80 \times 22$$

3.
$$30 \times 52$$

4.
$$60 \times 20$$

Problem Solving Real

- **5.** Octavio bought 20 packs of baseball cards. There are 12 cards in each pack. How many cards did Octavio buy?
- **6.** The Hart family drove 10 hours to their vacation spot. They drove an average of 48 miles each hour. How many miles did they drive?
- **7. WRITE** Math Write the steps for how to use a number line to multiply a 2-digit number by 20. Give an example.

Lesson Check

- **8.** For the school play, 40 rows of chairs are set up. There are 22 chairs in each row. How many chairs are there?
- **9.** At West School, there are 20 classrooms. Each classroom has 20 students. How many students are at West School?

Spiral Review

- 10. Samira has 48 stickers. This is 6 times the number of stickers Max has. How many stickers does Max have?
- **11.** Ali's dog weighs 8 times as much as her cat. Together, the two pets weigh 54 pounds. How much does Ali's dog weigh?

- **12.** Trinity has 3 containers with 25 crayons in each. She also has 4 boxes of markers with 12 markers in each box. She gives 10 crayons to a friend. How many crayons and markers does Trinity have now?
- **13.** The state of Utah covers 82,144 square miles. The state of Montana covers 145,552 square miles. What is the total area of the two states?

MTR.6.1

- (I Can) use different strategies to estimate products.
- Mathematical Thinking & Reasoning MTR.2.1, MTR.3.1, MTR.4.1, MTR.5.1,



■ UNLOCK the Problem



On average, the Smith family opens the door of their refrigerator 32 times each day. There are 31 days in May. About how many times is the refrigerator door opened in May?

Underline any information you will need.



One Way Use rounding and mental math.

Estimate. 31×32

STEP 1 Round each factor.

$$31 \times 32$$

STEP 2 Use mental math.

$$3 \times 3 = 9 \leftarrow \text{basic fact}$$

$$30 \times 30 =$$



MTR Engage in discussions on 4.1 mathematical thinking.

Is the exact product greater than or less than 900? Explain.

So, the Smith family opens the refrigerator door about 900 times during the month of May.

1. On average, a refrigerator door is opened 38 times each day. About how many fewer times in May is the Smith family's refrigerator door opened than the average refrigerator door?



All 24 light bulbs in the Saidi family's home are CFL light bulbs. Each CFL light bulb uses 28 watts to produce light. About how many watts will the light bulbs use when turned on all at the same time?

Another Way Use mental math and compatible numbers.

Compatible numbers are numbers that are easy to compute mentally.

Estimate. 24×28

STEP 1 Use compatible numbers.

$$25 \times 30$$
 Think: $25 \times 3 = 75$

So, about 750 watts are used.

STEP 2 Use mental math.

$$25 \times 3 = 75$$



Try This! Estimate $26 \times \$79$.

A Round to the nearest ten

B Compatible numbers

\$79 Think: How can you use
$$25 \times 4 = 100$$
 to

help find 25×8 ?

$$26 \times \$79$$
 is about .

- **2.** Explain why \$2,400 and \$2,000 are both reasonable estimates.
- **3.** In what situation might you choose to find an estimate rather than an exact answer?

Share and Show

Math

1. To estimate the product of 62 and 28 by rounding, how would you round the factors? What would the estimated product be?

2.
$$96 \times 34$$

$$\checkmark$$
 3. 47 × \$39

$$\checkmark$$
 4. 78×72



MTR Engage in discussions on 4.1 mathematical thinking.

How do you know if an estimated product will be greater than or less than the exact answer?

On Your Own

Estimate the product. Choose a method.

5.
$$41 \times 78$$

6.
$$51 \times 73$$

7.
$$34 \times 80$$

8.
$$61 \times 31$$

9.
$$52 \times 68$$

10.
$$26 \times 44$$

Find two possible factors for the estimated product.

12. 2,800

13. 8,100

14. 5,600

15. 2,400

- 16. Mr. Molefe jogs for 35 minutes each day. He jogs 5 days in week 1, 6 days in week 2, and 7 days in week 3. About how many minutes does he jog?
- 17. There are 48 beads in a package. Akelah bought 4 packages of blue, 9 packages of gold, 6 packages of red, and 2 packages of silver beads. About how many beads did Akelah buy?

Problem Solving · Applications World



- **18.** On average, a refrigerator door is opened 38 times each day. Kyler has two refrigerators in his house. Based on this average, about how many times in a 3-week period are the refrigerator doors opened?
- 19. The cost to run a refrigerator is about \$57 each year. About how much will it have cost to run by the time it is 15 years old?
- **20.** If Mel opens his refrigerator door 36 times every day, about how many times will it be opened in April? Will the exact answer be more than or less than the estimate? Explain.



21. MTR What question could you write for this answer? The estimated product of two numbers, that are not multiples of ten, is 2,800.

Show the Math

Demonstrate Your Thinking

- **22.** For numbers 22a 22d, select True or False for each sentence.
 - 22a. 26×48 is about 25×50 .
- false true
- 22b. 21×22 is about 20×30 .
- true false
- 22c. 28×21 is about 30×30 .
- false true
- 22d. 51×26 is about 50×25 .
- true
- false

Estimate Products by 2-Digit Numbers

Go Online

Interactive Examples

Estimate the product. Choose a method.

1. 38×21



800

4. 73×67

2. 63×19

5. 37 × \$44

3. $27 \times 42

6. 45×22

Problem Solving 🞇



- 7. A dime has a diameter of about 18 millimeters. About how many millimeters long would a row of 34 dimes be?
- 8. A half-dollar has a diameter of about 31 millimeters. About how many millimeters long would a row of 56 half-dollars be?

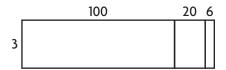
9. **WRITE** Math Describe a real-life multiplication situation for which an estimate makes sense. Explain why it makes sense.

Lesson Check

- **10.** What is a reasonable estimate for the product of 43 and 68?
- 11. Marissa burns 93 calories each time she plays fetch with her dog. She plays fetch with her dog once a day. About how many calories will Marissa burn playing fetch with her dog in 28 days?

Spiral Review

12. Use the model to find 3×126 .



13. A store sold a certain brand of jeans for \$38. One day, the store sold 6 pairs of jeans of that brand. How much did the 6 pairs of jeans cost?

- 14. The Gateway Arch in St. Louis, Missouri, weighs about 20,000 tons. Write an amount that could be the exact number of tons the Arch weighs.
- 15. What is another name for 23 ten thousands?

(I Can) use area models and partial products to multiply

Florida's B.E.S.T.

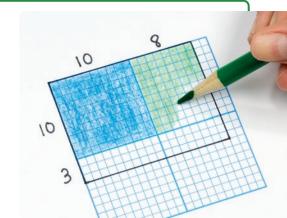
- Number Sense & Operations 4.NSO.2.2, 4.NSO.2.5
- Mathematical Thinking & Reasoning MTR.2.1, MTR.3.1, MTR.4.1, MTR.5.1, MTR.7.1

by 2-digit numbers.

Materials ■ color pencils

How can you use a model to break apart factors and make them easier to multiply?

A. Outline a rectangle on the grid to model 13 × 18. Break apart the model into smaller rectangles to show factors broken into tens and ones. Label and shade the smaller rectangles. Use the colors below.

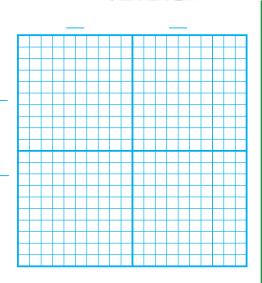


B. Find the product of each smaller rectangle. Then, find the sum of the partial products. Record your answers.

$$= 10 \times 10$$

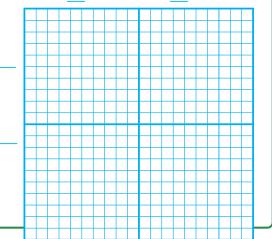
$$= 10 \times 8$$

$$=$$
 3×10



C. Draw the model again. Break apart the whole model to show factors different from those shown the first time. Label and shade the four smaller rectangles and find their products. Record the sum of the partial products to represent the product of the whole model.





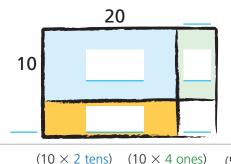
Draw Conclusion

- **1.** Explain how you found the total number of squares in the whole model.
- **2.** Compare the two models and their products. What can you conclude? Explain.
- **3.** To find the product of 10 and 33, which is the easier computation, $(10 \times 11) + (10 \times 11) + (10 \times 11)$ or $(10 \times 30) + (10 \times 3)$? Explain.

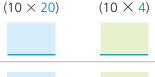
Make Connections

You can draw a simple diagram to model and break apart factors to find a product. Find 15×24 .

STEP 1 Draw a model to show 15×24 . Break apart the factors into tens and ones to show the partial products.



STEP 2 Write the product for each of the smaller rectangles.



 $(5 \times 2 \text{ tens})$ $(5 \times 4 \text{ ones})$

 $(5 \times 20) \qquad (5 \times 4)$

Remember

24 is 2 tens 4 ones.

STEP 3 Add to find the product for the whole model.



+ ____ =

So, $15 \times 24 = 360$.

The model shows four parts. Each part represents a partial product. The partial products are 200, 40, 100, and 20.

Math Engage in discussions on mathematical thinking.

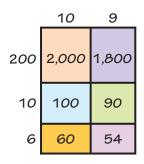
How does breaking apart the factors into tens and ones make finding the product easier?

Share and Show

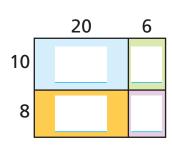
Math **Board**

Find the product.

1.
$$216 \times 19 =$$



2.
$$18 \times 26 =$$



2.
$$18 \times 26 =$$
 ______ **3.** $27 \times 39 =$ _____

	30	9
20		
7		

Draw a model to represent the product. Then record the product.

4.
$$14 \times 16 =$$

$$\checkmark$$
 5. $123 \times 25 =$

On Your Own

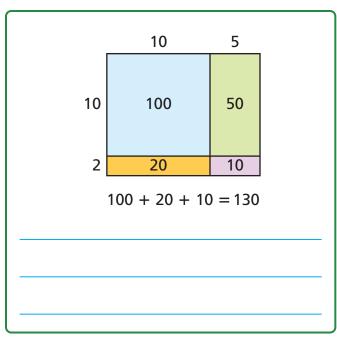
- **6. MTR** Explain how modeling partial products can be used to find the products of greater numbers.
- 7. Alleta bought 16 packages of rolls for a party. There were 12 rolls in a package. After the party there were 8 rolls left over. How many rolls were eaten? Explain.

Sense or Nonsense?

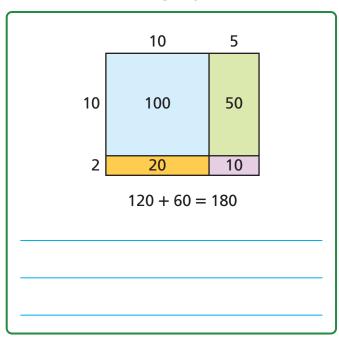


8. Jamal and Kim used different ways to solve 12×15 by using partial products. Whose answer makes sense? Whose answer is nonsense? Explain your reasoning.

Jamal's Work



Kim's Work



- **a.** For the answer that is nonsense, write an answer that makes sense.
- **b.** Look at Kim's method. Can you think of another way Kim could use the model to find the product? Explain.

10	5
100	50
20	10
	100

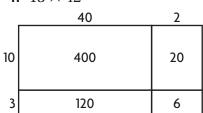
9. Look at the model in 8b. How would the partial products change if the product was 22 \times 15? Explain why you think the products changed.

Area Models and Partial Products

Go Online
Interactive Examples

Draw a model to represent the product. Then record the product.

1.
$$13 \times 42$$



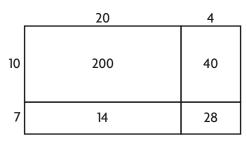
2.
$$418 \times 34$$

3.
$$22 \times 326$$

$$400 + 20 + 120 + 6 = 546$$

Problem Solving Real

4. Kalani made the following model to find the product of 17×24 .



$$200 + 40 + 14 + 28 = 282$$

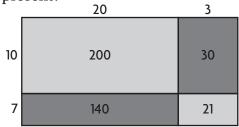
Is his model correct? Explain.

5. Each student in Ms. Haji's kindergarten class has a box of crayons. Each box has 36 crayons. If there are 18 students in Ms. Haji's class, how many crayons are there?

6. WRITE Math Describe how to model 2-digit by 2-digit multiplication using an area model.

Lesson Check

7. What product does the model below represent?



8. Find the product 524×63 . Use an area model.

Spiral Review

eat in 28 days?

- **9.** Beulah builds a tabletop using square tiles. There are 12 rows of tiles and 30 tiles in each row. How many tiles does Beulah use?
- 10. Asher bakes 8 batches of biscuits, with 14 biscuits in each batch. He sets aside 4 biscuits from each batch for a bake sale and puts the rest in a container. How many biscuits does Asher put in the container?

11. Li feeds her dog 3 cups of food each day. About how many cups of food does her dog

12. What is the product?

 $5,798 \times 6$

- Number Sense & Operations 4.NSO.2.2, 4.NSO.2.5
- Mathematical Thinking & Reasoning MTR.2.1, MTR.3.1, MTR.6.1, MTR.7.1

UNLOCK the Problem

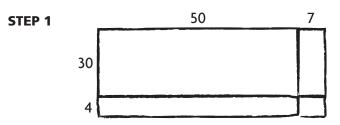
(I Can) use partial products to multiply.

You know how to break apart a model to find partial products. How can you use what you know to find and record a product?

Multiply. 34×57 Estimate. $30 \times 60 =$



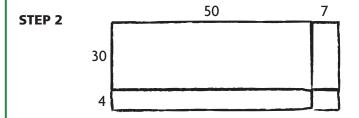
SHADE THE MODEL





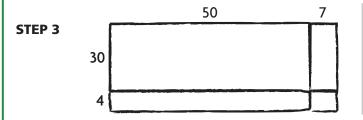
Multiply the tens by the tens. $30 \times 5 \text{ tens} = 150 \text{ tens}$

THINK AND RECORD

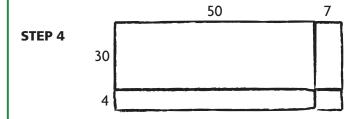




Multiply the ones by the tens. 30×7 ones = 210 ones



- **57** $\times 34$ 1,500 210
- Multiply the tens by the ones. 4×5 tens = 20 tens



210 200

1,500

57 \times 34

> Multiply the ones by the ones. 4×7 ones = 28 ones Add the partial products.

So, $34 \times 57 = 1,938$. Since 1,938 is close to the estimate of 1,800, it is reasonable.



MTR Complete tasks with 3.1 mathematical fluency.

You can write 10×4 ones = 40 ones as $10 \times 4 = 40$. What is another way to write 10×3 tens = 30 tens?

Example

The apples from each tree in an orchard can fill 23 bushel baskets. If 1 row of the orchard has 48 trees, how many baskets of apples can be filled?

Multiply. 48×23

Estimate.
$$50 \times 20 =$$

THINK

RECORD

STEP 1

Multiply the tens by the tens.



← 40 × _____ tens = ____ tens

STEP 2

Multiply the ones by the tens.



← 40 × _____ ones = ____ ones

STEP 3

Multiply the tens by the ones.

23 × 48

800 120

← 8 × _____ tens = ____ tens

STEP 4

Multiply the ones by the ones. Then add the partial products.

23

160

← 8 × _____ ones = ____ ones

MTR Assess reasonableness **6.1** of solutions.

How do you know your answer is reasonable?

Share and Show

So, 1,104 baskets can be filled.

1. Find 24×34 .

	30	4
20	600	80
4	120	16



Record the product.

$$\begin{array}{c|c}
\checkmark 5. & 437 \\
\times & 26
\end{array}$$

On Your Own

Record the product.

10.
$$38 \times 47$$

11.
$$46 \times 27$$

12.
$$724 \times 53$$

13.
$$98 \times 169$$

14.
$$53 \times 682$$

15.
$$976 \times 84$$

16.
$$92 \times 48$$

17.
$$37 \times 79$$

MTR Find the unknown digits. Complete the problem.

$$\begin{array}{c|c}
 & 6 \\
 \times & 4 \\
\hline
 1,400 \\
 120 \\
 280 \\
 + 24
\end{array}$$

$$\begin{array}{c|c}
 & 2 \\
 \times & 7 \\
 \hline
 7,200 \\
 180 \\
 560 \\
 + & 14
\end{array}$$

$$\begin{array}{r}
 \times 5 \\
 \hline
 1,500 \\
 300 \\
 90 \\
 + 18
 \end{array}$$

3

Problem Solving · Applications Work

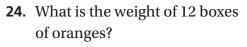


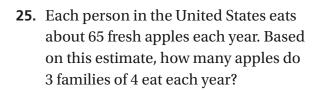
Use the pictograph for 22-24.

22. MTR A fruit-packing warehouse is shipping 15 boxes of grapefruit to a store in Santa Rosa, California. What is the total weight of the shipment?

23.	How much less do 13 boxes
	of tangelos weigh than 18 boxes
	of tangerines?

of tangerines?	





26.	The product 26×493 is greater than
	25×493 . How much greater? Explain how
	you know without multiplying.

Pounds of Citrus Fruit per Box							
Citrus Fruit	Weight per Box (in pounds)						
Grapefruit	33333334						
Orange							
Tangelo							
Tangerine	•••••						
	Voy: Each 🤼 10 nounds						

Key: Each \bigcirc = 10 pounds.

Show the Math

Demonstrate Your Thinking



27. Moesha wants to use partial products to find 22×17 . Write the numbers in the boxes to show 22×17 .

Multiply Using Partial Products

Go Online
Interactive Examples

Record the product.

+ 27 1,817

Problem Solving Real

- **8.** Evelyn drinks 8 glasses of water a day, which is 56 glasses of water a week. How many glasses of water does she drink in a year? (1 year = 52 weeks)
- 9. Cato wants to use the Hiking Club's funds to purchase new walking sticks for each of its 19 members. The sticks cost \$26 each. The club has \$480. Is this enough money to buy each member a new walking stick? If not, how much more money is needed?

10. WRITE *Math* Explain why it works to break apart a number by place values to multiply.

Lesson Check

- 11. A carnival snack booth made \$76 selling popcorn in one day. It made 22 times as much selling cotton candy. How much money did the snack booth make selling cotton candy?
- **12.** List the partial products of 242 and 28.

Spiral Review

- **13.** Last year, the city library collected 117 used books for its shelves. This year, it collected 3 times as many books. How many books did it collect this year?
- **14.** Washington Elementary has 232 students. Washington High has 6 times as many students. How many students does Washington High have?

- **15.** List the partial products of 35 and 7.
- **16.** Camille has ten \$5 bills and thirteen \$10 bills. How much money does Camille have in all?

Multiply with Regrouping

(I Can) use regrouping to multiply whole numbers.

Lesson 5

Florida's B.E.S.T.

- Number Sense & Operations 4.NSO.2.2, 4.NSO.2.5
- Mathematical Thinking & Reasoning MTR.2.1, MTR.3.1, MTR.4.1, MTR.5.1, MTR.6.1, MTR.7.1

▲ The first production Model T Ford

was assembled on October 1, 1908.



UNLOCK the Problem World

By 1914, Henry Ford had streamlined his assembly line to make a Model T Ford car in 93 minutes. How many minutes did it take to make 25 Model Ts?

Use place value and regrouping.

Multiply.
$$93 \times 25$$
 Estimate. $90 \times 30 =$

THINK RECORD

STEP 1

- Think of 93 as 9 tens and 3 ones.
- Multiply 25 by 3 ones.

1 25

 \leftarrow 3 \times 25



• Multiply 25 by 9 tens.



 \leftarrow 90 \times 25

STEP 3

• Add the partial products.

+2,250

So, 93×25 is 2,325. Since _____ is close

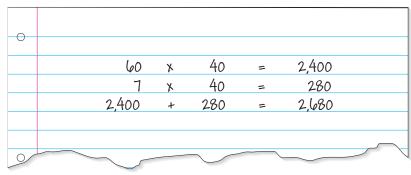
to the estimate of _____, the answer is reasonable.



MTR Engage in discussions on 4.1 mathematical thinking.

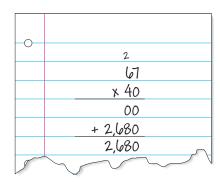
Why do you get the same answer whether you multiply 93×25 or 25×93 ? **Different Ways to Multiply** You can use different ways to multiply and still get the correct answer. Cyrus and Kasra both solved 67×40 correctly, but they used different ways.

Look at Cyrus' paper.



So, Cyrus' answer is $67 \times 40 = 2,680$.

Look at Kasra's paper.



So, Kasra also found $67 \times 40 = 2,680$.

- 1. What method did Cyrus use to solve the problem?
- **2.** What method did Kasra use to solve the problem?

Share and Show Bogrd

1. Look at the problem. Complete the sentences.

Multiply _____ and ____ to get 0.

Multiply _____ and ____ to get 1,620.

Add the partial products.

$$0 + 1,620 =$$

$$\frac{\times 60}{0}$$

+1,620

Estimate. Then find the product.

2. Estimate:

⋖ 3. Estimate: ___

4. Estimate:



MTR Complete tasks with 3.1 mathematical fluency.

Why can you omit zeros of the first partial product when you multiply 20 \times 34?

On Your Own

Estimate. Then find the product.

5. Estimate:

$$30$$
 \times 47

6. Estimate:

$$278$$
 \times 56

7. Estimate: _____

$$27 \times 25$$

- **8.** 34×65
- **9.** $142 \times 13
- **10.** 60×17
- **11.** 462×45 **12.** $57 \times \$98$

MTR Write a rule for the pattern. Use your rule to find the unknown numbers.

13.

Hours	h	5	10	15	20	25
Minutes	m	300	600	900		

- **14.** Owners of a summer camp are buying new cots for their cabins. There are 16 cabins. Each cabin needs 6 cots. Each cot costs \$92. How much will the new cots cost?
- 15. A theater has 28 rows of 38 seats downstairs and 14 rows of 26 seats upstairs. How many seats does the theater have?

Problem Solving · Applications World



16. Machine A can label 11 bottles in 1 minute. Machine B can label 12 bottles in 1 minute. How many bottles can both machines label in 15 minutes?





- a. What do you need to know?
- **b.** What numbers will you use?
- **c.** Tell why you might use more than one operation to solve the problem.
- **d.** Solve the problem.

So, both machines can label _____ bottles

in _____ minutes.

- **17.** MTR A toy company makes wooden blocks. A carton holds 85 blocks. How many blocks can 19 cartons hold?
- **18.** A company is packing cartons of candles. Each carton can hold 75 candles. So far, 50 cartons have been packed, but only 30 cartons have been loaded on a truck. How many more candles are left to load on the truck?
- 19. Mr. Garcia's class raised money for a field trip to the zoo. There are 23 students in his class. The cost of the trip will be \$17 for each student. What is the cost for all the students? Explain how you found your answer.

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Multiply with Regrouping

Go Online Interactive Examples

Estimate. Then find the product.

Think: 87 is close to 90 and 32 is close to 30.

$$90 \times 30 = 2,700$$

2.	Estimate:	

$$673$$
 \times 28

$$359$$
 \times 52

Problem Solving Real Work

- **5.** Baseballs come in cartons of 84 baseballs. A team orders 18 cartons of baseballs. How many baseballs does the team order?
- **6.** There are 16 tables in the school lunch room. Each table can seat 22 students. How many students can be seated at lunch at one time?

7. **WRITE** Math Write about which method you prefer to use to multiply two 2-digit numbers—regrouping, partial products, or breaking apart a model. Explain why.

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Lesson Check

- **8.** The art teacher has 48 boxes of crayons. There are 64 crayons in each box. How many crayons does the teacher have?
- 9. A basketball team scored an average of 52 points in each of 15 games. Based on the average, how many points did the team score in all?

Spiral Review

- 10. One Saturday, an orchard sold 83 bags of apples. There are 27 apples in each bag. About how many apples were sold?
- 11. Deja has a grid of squares that has 12 rows with 15 squares in each row. She colors 5 rows of 8 squares in the middle of the grid blue. She colors the rest of the squares red. How many squares does Deja color red?

- **12.** Gabriella has 4 times as many erasers as Leona. Leona has 8 erasers. How many erasers does Gabriella have?
- **13.** Jun has 3 times as many rocks as Heechul. Together, they have 48 rocks. How many more rocks does Jun have than Heechul?

Florida's B.E.S.T.

- Number Sense & Operations 4.NSO.2.2, 4.NSO.2.5, 4.NSO.2.3
- Mathematical Thinking & Reasoning MTR.2.1, MTR.3.1, MTR.4.1, MTR.5.1, MTR.7.1

Choose a Multiplication Method

I Can use multiple strategies to multiply 2-digit and 3-digit numbers by 2-digit numbers.

\blacksquare UNLOCK the Problem $rac{Rea}{Wor}$

Did you know using math can help prevent you from getting a sunburn?

The time it takes to burn without sunscreen multiplied by the SPF, or sun protection factor, is the time you can stay in the sun safely with sunscreen.

If today's UV index is 8, Hua will burn in 15 minutes without sunscreen. If Hua puts on lotion with an SPF of 25, how long will she be protected?

One Way Use partial products to find 15×25 .

$$\begin{array}{c}
25 \\
\times 15
\end{array}$$

$$\leftarrow 10 \times 2 \text{ tens} = 20 \text{ tens}$$

$$\leftarrow 10 \times 5 \text{ ones} = 50 \text{ ones}$$

$$\leftarrow 5 \times 2 \text{ tens} = 10 \text{ tens}$$

$$\leftarrow 5 \times 5 \text{ ones} = 25 \text{ ones}$$

$$\leftarrow \text{Add.}$$

- Underline the sentence that tells you how to find the answer.
- Circle the numbers you need to use. What operation will you use?



▲ Sunscreen helps to prevent sunburn.



Draw a picture to check your work.

So, if Hua puts on lotion with an SPF of 25, she will be protected for $375\,\mathrm{minutes}$.



MTR Engage in discussions on 4.1 mathematical thinking.

Explain how it was easier to find the product using partial products.

Another Way Use regrouping to find 15 \times 25.

Estimate. $20 \times 20 =$

STEP 1

Think of 15 as 1 ten 5 ones. Multiply 25 by 5 ones, or 5.

STEP 2

Multiply 25 by 1 ten, or 10.

$$\begin{array}{r}
\stackrel{2}{\cancel{25}} \\
\times 15 \\
\hline
125 \\
\leftarrow 10 \times 25
\end{array}$$

Add the partial products.

Try This! Multiply. $57 \times \$43$

Estimate. $57 \times 43

Use	Use partial products.					Us	e re	grou	ıpin	g.		
			\$	4	3				\$	4	3	
		×		5	7			×		5	7	

- 1. How do you know your answer is reasonable?
- **2.** Look at the partial products and regrouping methods above. How are the partial products 2,000 and 150 related to 2,150?

How are the partial products 280 and 21 related to 301?

1. Find the product.

		5	4	
×		2	9	
	×	X		



MTR Engage in discussions on 4.1 mathematical thinking.

Why do you begin with the ones place when you use the regrouping method to multiply?

Estimate. Then choose a method to find the product.

2. Estimate:

236 \times 14 **3.** Estimate:

 \times 42

⊘4. Estimate: _____

384 \times 53 **5.** Estimate:

71 \times 13

On Your Own

Estimate. Find the product.

7.
$$357 \times 79$$

8.
$$80 \times 27$$

10.
$$655 \times 48$$

12.
$$925 \times $25$$

13.
$$41 \times 98$$

MTR Use mental math to find the number.

14.
$$30 \times 14 = 420$$
, so $30 \times 15 =$ ____.

14.
$$30 \times 14 = 420$$
, so $30 \times 15 =$ _____ = 350.

- **16.** MTR The town conservation manager bought 16 maple trees for \$26 each. She paid with five \$100 bills. How much change will the manager receive? Explain.
- 17. Each of 25 students in Group A read for 45 minutes. Each of 21 students in Group B read for 48 minutes. Which group read for more minutes? Explain.

Problem Solving · Applications



18. Martin collects stamps. He counted 48 pages in his collector's album. The first 20 pages each have 35 stamps in 5 rows. The rest of the pages each have 54 stamps. How many stamps does Martin have in his album?





- a. What do you need to know?
- **b.** How will you use multiplication to find the number of stamps?
- **c.** Tell why you might use addition and subtraction to help solve the problem.

- **d.** Show the steps to solve the problem.
- e. Complete the sentences.

Martin has a total of stamps on the first 20 pages.

There are more pages after the first 20 pages in Martin's album.

There are stamps on the rest of the pages.

There are _____stamps in the album.

19. Select the expressions that have the same product as 35×17 . Mark all that apply.

$$\circ$$
 (30 × 10) + (30 × 7) + (5 × 10) + (5 × 7) \circ (30 × 17) + (5 × 17)

$$\circ$$
 (30 × 17) + (5 × 17)

$$\circ$$
 (35 × 30) + (35 × 5) + (35 × 10) + (35 × 7) \circ (35 × 10) + (35 × 7)

$$\circ$$
 (35 × 10) + (35 × 7)

$$\circ$$
 (35 × 10) + (30 × 10) + (5 × 10) + (5 × 7) \circ (35 × 30) + (35 × 5)

$$\circ$$
 (35 × 30) + (35 × 5)

Choose a Multiplication Method

Go Online Interactive Examples

Estimate. Then choose a method to find the product.

1. Estimate: <u>1,200</u>

3. Estimate:

$$\begin{array}{r}
 31 \\
 \times 43 \\
\hline
 93 \\
 + 1,240 \\
\hline
 1,333
\end{array}$$

$$\begin{array}{r} 67 \\ \times 85 \end{array}$$

$$\begin{array}{r} 368 \\ \times 38 \end{array}$$

$$\begin{array}{r} 449 \\ \times 54 \end{array}$$

$$91$$
 \times 26

$$282$$
 \times 19

Problem Solving Rea

- 8. A movie theatre has 26 rows of seats. There are 18 seats in each row. How many seats are there?
- 9. Each class at Briarwood Elementary collected at least 54 cans of food during the food drive. If there are 29 classes in the school, what was the least number of cans collected?
- **10. WRITE** Math How is multiplication using partial products different from multiplication using regrouping? How are they similar?

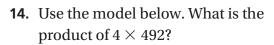
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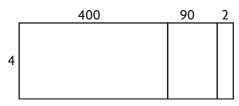
Lesson Check

- 11. A choir needs new robes for each of its 46 singers. Each robe costs \$32. What will be the total cost for all 46 robes?
- **12.** A wall on the side of a building is made up of 152 rows of bricks with 44 bricks in each row. How many bricks make up the wall?

Spiral Review

13. Write an expression that shows how to multiply 4×362 using place value and expanded form.





15. What is the sum 13,094 + 259,728?

16. During the 2019–2020 season, there were 18,391 people who attended the home hockey games in Philadelphia. There were 14,606 people who attended the home hockey games in Phoenix. How much greater was the home attendance in Philadelphia than in Phoenix that season?

Multiply by 2-Digit Numbers

(I Can) solve real-world problems using multiplication.

Florida's B.E.S.T.

- Algebraic Reasoning 4.AR.1.1
- Number Sense & Operations 4.NSO.2.3
- Mathematical Thinking & Reasoning MTR.2.1, MTR.4.1, MTR.6.1, MTR.7.1



🔡 UNLOCK the Problem Real



During the 2010 Great Backyard Bird Count, an average of 42 bald eagles were counted in each of 20 locations throughout Alaska. In 2009, an average of 32 bald eagles were counted in each of 26 locations throughout Alaska. Based on this data, how many more bald eagles were counted in 2010 than in 2009?

Use the graphic organizer to help you solve the problem.



Read the Problem

What do I need to find?

I need to find bald eagles were counted in 2010 than in 2009.

What information do I need to use?

In 2010, _____ locations counted an average of ____ bald eagles each. In 2009, locations counted an average of

How will I use the information?

I can solve simpler problems.

____ bald eagles each.

Find the number of bald eagles counted in _____.

Find the number of bald eagles counted in _____.

Then draw a bar model to compare the _____

count to the ____ count.

Solve the Problem

• First, find the total number of bald eagles counted in 2010.

×

- = ____ bald eagles counted in 2010
- Next, find the total number of bald eagles counted in 2009.

= \times

- = ____ bald eagles counted in 2009
- Last, draw a bar model. I need to subtract.

840 bald eagles in 2010

832 bald eagles in 2009

840 - 832 =

So, there were more bald eagles counted in 2010 than in 2009.

Try Another Problem

Prescott Valley, Arizona, reported a total of 29 mourning doves in the Great Backyard Bird Count. Mesa, Arizona, reported 20 times as many mourning doves as Prescott Valley. If Chandler reported a total of 760 mourning doves, how many more mourning doves were reported in Chandler than in Mesa? Mourning dove ▶



Read the Problem	Solve the Problem
What do I need to find?	
What information do I need to use?	
	760 mourning doves in Chandler
How will I use the information?	580 mourning doves in Mesa?

Engage in discussions on 4.1 mathematical thinking.

What is another way you could solve this problem?

Is your answer reasonable? Explain.

Share and Show

Math Board

✓ 1. An average of 74 reports with bird counts were turned in each day in June. An average of 89 were turned in each day in July. How many reports were turned in for both months? (Hint: There are 30 days in June and 31 days in July.)

First, write the problem for June.

Next, write the problem for July.

Last, find and add the two products.

reports were turned in for both months.

✓ 2. What if an average of 98 reports were turned in each day for the month of June? How many reports were turned in for June? Describe how your answer for June would be different.

- **3.** There are 48 crayons in a box. There are 12 boxes in a carton. Mr. Chou ordered 11 cartons of crayons for the school. How many crayons did he get?
- **4.** MTR Each of 8 bird-watchers reported seeing 15 roseate spoonbills in a day. If they each reported seeing the same number of roseate spoonbills over 14 days, how many would be reported?



Show the Math

Demonstrate Your Thinking

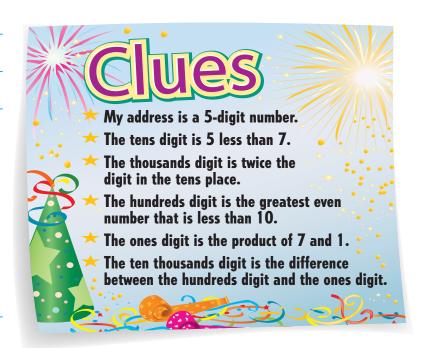
On Your Own

5. On each of Maggie's bird-watching trips, she has seen at least 24 birds. If she has taken 4 of these trips each year over the past 16 years, at least how many birds has Maggie seen?



6. MTR There are 12 inches in a foot. In September, Mrs. Baeza orders 64 feet of ribbon for the Crafts Club. In January, she orders 9 feet less. How many inches of ribbon does Mrs. Baeza order? Explain how you found your answer.

7. Ekta is having a party on Saturday. She decides to write a riddle on her invitations to describe her house number on Cypress Street. Use the clues to find Ekta's address.



8. A school is adding 4 rows of seats to the auditorium. There are 37 seats in each row. Each new seat costs \$99. What is the total cost for the new seats? Show your work.

Multiply by 2-Digit Numbers

Go Online **Interactive Examples**

Solve each problem. Use a bar model to help.

1. Oleg counted an average of 18 birds at his bird feeder each day for 20 days. Vera counted an average of 21 birds at her bird feeder each day for 16 days. How many more birds did Oleg count at his feeder than Vera counted at hers?

Birds counted by Oleg: $18 \times 20 = 360$

Birds counted by Vera: $21 \times 16 = 336$

Draw a bar model to compare.

Subtract. 360 - 336 = 24

360 birds counted by Oleg 336 birds counted by Vera

So, Oleg counted <u>24</u> more birds.

- 2. The 24 students in Ms. Lee's class each collected an average of 118 cans for recycling. The 21 students in Mr. Galvez's class each collected an average of 125 cans for recycling. How many more cans were collected by Ms. Lee's class than Mr. Galvez's class?
- 3. At East School, each of the 45 classrooms has an average of 22 students. At West School, each of the 42 classrooms has an average of 23 students. How many more students are at East School than at West School?
- **4. WRITE** Math Draw a bar model that shows how the number of hours in March compares with the number of hours in February of this year.

Lesson Check

- **5.** Ace Manufacturing ordered 17 boxes with 105 ball bearings each. They also ordered 15 boxes with 90 springs each. How many more ball bearings than springs did they order?
- **6.** Elton hiked 16 miles each day on a 12-day hiking trip. Lola hiked 14 miles each day on her 16-day hiking trip. In all, how many more miles did Lola hike than Elton hiked?

Spiral Review

- **7.** An orchard has 24 rows of apple trees. There are 35 apple trees in each row. How many apple trees are in the orchard?
- 8. An amusement park reported 354,605 visitors last summer. What is this number rounded to the nearest thousand?

- **9.** Attendance at the football game was 102,653. What is the value of the digit 6?
- 10. Jill's fish weighs 8 times as much as her parakeet. Together, the pets weigh 63 ounces. How much does the fish weigh?

Chapter Review

1. Explain how to find 40×50 using mental math.

2. Mrs. Traynor's class is taking a field trip to the zoo. The trip will cost \$26 for each student. There are 22 students in her class.

Part A

Round each factor to estimate the total cost of the students' field trip.

Part B

Use compatible numbers to estimate the total cost of the field trip.

Part C

Which do you think is the better estimate? Explain.

3. For Problems 3a–3e, select Yes or No to show if the answer is correct.

3a. $35 \times 10 = 350$

○ Yes ○ No

3b. $19 \times 20 = 380$

○ Yes ○ No

3c. $12 \times 100 = 120$

○ Yes ○ No

3d. $70 \times 100 = 7,000$

○ Yes ○ No

3e. $28 \times 30 = 8,400$

○ Yes ○ No

4. There are 23 boxes of pencils in Mr. Shaw's supply cabinet. Each box contains 100 pencils. How many pencils are in the supply cabinet?

_____pencils

5. Which would provide a reasonable estimate for each product? Write the estimate beside the product. An estimate may be used more than once.

50 × 20

 25×40

 30×30

 23×38

 46×18

 31×32

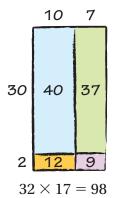
 39×21

6. There are 26 baseball teams in the league. Each team has 18 players. Write an equation that will provide a reasonable estimate for the number of players in the league. Explain how you found your estimate.



7. The model shows 489 \times 37. Write the partial products.

8. Jess made this model to find the product of 32×17 . Her model is incorrect.

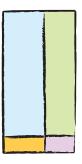


Part A

What did Jess do wrong?

Part B

Redraw the model so that it is correct.



Part C

What is the actual product of 32×17 ?

9. Tatum wants to use partial products to find 15×32 . Write the numbers in the boxes to show 15×32 .

10. Which product is shown by the model? Write the letter of the product on the line below the model.





$$\bigcirc$$
 13 × 13

	10	3
10	100	30
3	30	9

	10	4
20	200	80
4	40	16

11. Mrs. Jones places 3 orders for school T-shirts. Each order has 16 boxes of shirts, and each box holds 17 shirts. How many T-shirts does Mrs. Jones order? Use partial products to help you.

12. Write the unknown digits. Use each digit exactly once.

13. Mohammed has logged 216 minutes in the school-wide reading competition. Francisco has 17 times as many minutes as Mohammed does. How many minutes does Francisco have?

_____ minutes

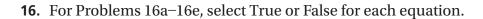
6

8

14. Multiply.

$$436 \times 28 =$$

15. A farmer planted 42 rows of tomatoes with 13 plants in each row. He planted 23 rows of corn with 21 plants in each row. How many more tomato plants did he plant than corn plants?



16a.
$$25 \times 18 = (20 \times 10) + (20 \times 8) + (5 \times 10) + (5 \times 8)$$

O True O False

16b.
$$25 \times 18 = (25 \times 20) + (25 \times 5) + (25 \times 10) + (25 \times 8)$$

O True O False

16c.
$$25 \times 18 = (20 \times 18) + (5 \times 10) + (5 \times 8)$$

○ True ○ False

16d.
$$25 \times 18 = (25 \times 10) + (25 \times 8)$$

O True O False

16e.
$$25 \times 18 = (25 \times 20) + (25 \times 5)$$

O True O False

17. Terrell runs 15 sprints. Each sprint is 165 meters. How many meters does Terrell run? Show your work.

18. There are 3 new seats in each row in a school auditorium. There are 15 rows in the auditorium. Each new seat cost \$74. What is the cost for the new seats? Explain how you found your answer.

19. Ray and Ella helped move their school library to a new building. Ray packed 27 boxes with 25 books in each box. Ella packed 23 boxes with 30 books in each box. How many more books did Ella pack? Show your work.

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	Part A
	Julius' answer is incorrect. What did Julius do wrong?
	Part B
	What did Walt do wrong?
	Part C
What is the correct product?	
	A clothing store sells 26 shirts and 22 pairs of jeans. Each item of clothing costs \$32.
	Part A
	What is a reasonable estimate for the total cost of the clothing? Show or explain how you found your answer.

What is the exact answer for the total cost of the clothing? Show or

Julius

 \times 16 150

+ 250

500

25

Walt

25 \times 16

200

50 120

<u>+ 300</u> 670

explain how you found your answer.